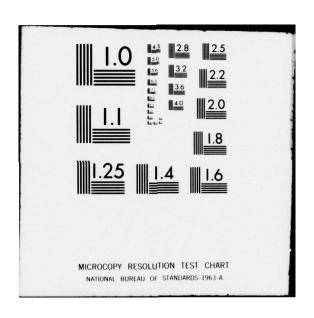
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AN INTERACTIVE ANALYSIS PROGRAM FOR A DIGITAL IMAGE PROCESSING LABORATORY

THESIS

AFIT/GE/EE/78S-16

Dennis A. McGaugh Capt USA.



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JOSEPH P. HIPPS, Major, USAF! Director of Information 19. Jan 79 AFIT/GE/EE/78S-16

AN INTERACTIVE ANALYSIS PROGRAM FOR A DIGITAL IMAGE PROCESSING LABORATORY

THESIS 9 Master's thesis,

Presented to the Faculty of the School of Engineering of the Air Force Institute of Technology

> Air University (ATC) in Partial Fulfillment of the Requirements for the Degree of Master of Science

-	by	
10	Dennis A./McGa	augh B.S.
	Capt.	USA

Graduate Electrical Engineering September 178

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Preface

This work attempts to provide the solution to a problem first identified by Major J. W. Carl of the Air Force Institute of Technology, School of Engineering. The basic problem was to design and implement the software necessary to allow two-dimensional linear filter and two-dimensional Discrete Fourier Transform (DFT) to be performed on an existing minicomputer-based image processing system. With the addition of the routines described in this thesis, true linear filtering of images is now available on the DICOMED Image Processing System. It is hoped that with its filtering capability, and with its 64x64 DFT capability that this new image analysis software will indeed provide a useful analytical tool.

I would like to take this brief opportunity to thank the people without whom this project would have been virtually impossible. Thanks to Captain Fred Barney for his making the DICOMED equipment available and for his patient explanations on the intracacier of same.

A special thanks to my thesis advisor, Major Carl for his saint-like patience and profound guidance during some very trying times. And lastly, but by no means least, thanks to my wife Marla for her typing the thesis rough draft and for her inspirational moral support.

Dennis A. McGaugh

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Abstract

A FORTRAN program is presented that will interactively prepare digitized images (pictures) for experimental analysis. The digital preparation includes the ability to Discrete Fourier Transform (DFT), Inverse Fourier Transform (IDFT), threshold image power spectral density, and to perform two-dimensional image filtering. Further, a brief discussion of image distortion measurements, optimal image size for experimental presentation, and image aliasing is provided. A sample of typical processed image results is also supplied.

AN INTERACTIVE ANALYSIS PROGRAM FOR A DIGITAL IMAGE PROCESSING LABORATORY

I. Introduction

There currently exists, located in the Air Force Avionics Laboratory, image processing hardware and software capable of digitizing and performing limited statistical calculations of pictorial imagery. There also exists a requirement to perform certain image processing with this equipment in preparation for a visual experiment. However, the software needed to conduct the processing did not formerly exist. The types of computations needed to perform this processing and analysis are well-known. But these computations needed to be developed in software and implemented on the particular small computer system that is available.

The image processing functions that are needed include: two-dimensional linear filtering, calculation of a two-dimensional image power spectrum, ability to specify a threshold for this power spectrum, and the Mean-Square-Error (MSE) and Bandwidth (BW) of an image constrained to occupy only those frequencies at which the power spectrum is above a specified threshold. Additionally, it is desired that these functions be interactively controlled and specified to the program during run time.

The problem is to develop and provide a software program capable of accomplishing the above functions, and still

be compatible with the existing equipment. Additionally, part of this thesis work is to determine what is the minimum size of picture digitization (e.g. 64x64, 128x128, 256x256) that will produce pictures suitable for the experiment; that is, a picture that creates an image of no less quality than 30 lines per 1° of visual angle subtended during viewing. The picture digitization will also impact on the computer resources needed to perform the filtering. The experiment currently calls for the use of up to 24 different pictures. These pictures are available in positive or negative form, and have been digitized (2048x2048) and stored on magnetic tape. The sampling resolution may also cause image aliasing problems, and this effect must also be discussed.

The material presented in this thesis follows roughly the same order as discussed above. Chapter II discusses the constraining environment, its effect on program development, and the digital domain for implementation of the required functions. Chapter III briefly describes the laboratory hardware/software and the final project software. Chapter IV presents a sample of processed image results, and Chapter V closes with summary remarks and mention of areas for future work. The appendix contains a program user's guide and complete program documentation.

II. Discussion

During the development of the image analysis program, several important questions had to be answered. The answers to some are rather straight-forward; the answers to others were influenced by answers to previous questions. The answer to each question, and its impact on the design of the image analysis program is presented in the section that follows. After reading these sections, it is hoped that there will be clear understanding of the program constraint enviropment.

A Question of Image Resolution

The requirement exists to conduct visual experiments with pictorial presentation to human subjects. The images should fall within the subjects' regions of foveal vision; that is, the images should not exceed a visual angle of 2 degrees during viewing. In discussions with (then) Captain Larry Goble of the US Air Force Flight Dynamics Laboratory at Wright-Patterson AFB, Ohio, the point was made that the industry standard for images on graphics and television displays is a twelve-inch square picture viewed at a distance of thirty inches with a resolution of no less than sixty lines per inch. It was also decided that this should be the resolution standard for the analysis program. After some basic geometrical calculations, this works out to be 30 lines of resolution per 1 visual degree (vis). Additionally, the experimental displays require that each visual presentation

consist of two different pictures placed side-by-side. Considering the overall limit of 2° vis vertically and horizontally, this means that for square pictures, each picture can only subtend 1° vis.

The answer to the question of image resolution is that each picture, in order to subtend 1° vis, must be 1/2 inch x 1/2 inch at 30 inches distance from the viewer, and each picture must have a minimum of 30 lines of resolution both horizontally and vertically. Imagery of this quality is obtainable through the use of the laboratory DICOMED image processing equipment. It should be noted, however, that the requirement for number of lines of resolution increases when considering the question of aliasing.

A Question of Aliasing in Digitized Images

The DICOMED image processing equipment digitizes a given picture with a sequential horizontal scanning action. It begins at the top of the picture to be digitized with a horizontal scan the width of the picture. It then proceeds incrementally down the picture with successive, picture width, horizontal scans until it stops at the picture bottom. Both horizontal and vertical directions are discretely sampled with an adjustable number of samples per picture widths (independently chosen in each direction). The result of this scanning process is the mapping of the entire picture into a MxN matrix of M·N discrete pixel values, where M and N are both powers of two. In this application, M was equal

to N. For the DICOMED machine, the value of each pixel can be any one of 256 gray scale levels, from white (377_8) to black (000_8) . When referring to the resolution of this resulting digitized picture, it is said to have N lines of resolution, with a sampling rate of N (where N=2^P).

The answer to the question of aliasing can be found by referring to the Nyquist sampling theorm (12:68). Restated, it simply says: to eliminate spectrum aliasing in the discrete domain, sample at a rate greater than or equal to twice the spectral width. Therefore, for the previous case of an NxN sampled image, in order to prevent aliasing after discrete Fourier transformations, there must not be any spatial-frequency content above $\frac{N}{2}$ cycles per picture The experimental requirement is for a minimum of 30 lines resolution per picture. This means that a digitized picture with this resolution can display up to 30 full oscillations (cycles) between white and black per picture in either the horizontal or vertical direction. Therefore, the display resolution criterion is satisfied if $\frac{N}{2} \ge 30$. Since a DFT/FFT computer algorithim (discussed later) will be used to transform into the Fourier domain, and powers of two run fastest in that algorithim, and since the DICOMED image processing system samples at powers of two, a sampling rate of 64 was selected as the minimum convenient value that N can have and still meet the display resolution criteria. This requires a 64x64 digitization of each image to be processed, and insures that, at this digitization level, the

resolution limits of human observers will be met under the cited viewing conditions.

Now, to insure no image aliasing, it must be guaranteed that there is no spatial frequency, in the image being transformed, above 32 cycles per picture width. To provide this guarantee, all 64x64 digital images used in this work were derived from pictures sampled at a rate much higher than 64 samples per line. The original pictures were first digitized into 2048x2048 images. Then by considering 64x64 blocks of 32x32 pixels, each 32x32 pixel block was averaged into one pixel value. The resultant averaged pixel values produce the required 64x64 digital image. In essence, this procedure performs a two-dimensional, digital low-pass filtering operation on a picture that may contain spatial frequencies of up to 1024 cycles. Although this type of lowpass filtering results in a $\frac{\sin x}{x}$ form for the filter in the frequency domain, and such filters are not particularly good in the stop-band of the filter (considerable side-lobe structure), these effects were ignored since relatively low spatial frequencies are anticipated in the original pictures. This procedure is essentially a digital simulation of the low-pass filtering operation necessary to avoid aliasing.

The Question of Linear Filtering Implementation

The functional requirement for linear filtering implies spatial convolution of the form (10:440): $y(n_1,n_2) = x(n_1,n_2) * h(n_1,n_2) = \underbrace{\begin{array}{c} 0 \\ m_1=-0c \end{array}}_{m_2=-0c} x(m_1,m_2).$

 $h(n_1-m_1, n_2-m_2)$

where $y(n_1,n_2)$ is the output image result of the $x(n_1,n_2)$ input image that has been filtered by a linear filter with an impulse response of $h(n_1,n_2)$. As noted by Rabiner and Gold (Ref 10), this calculation in the spatial domain with images is not usually soluable in closed form except for the most trivial filters. However, a more tractable form of this convolution equation occurs in the frequency domain. It is well-known (Ref 8) that the convolution equation takes the form:

 $Y(k_1,k_2) = X(k_1,k_2) \cdot H(k_1, k_2)$

where Y(k₁,k₂), X(k₁,k₂), and H(k₁,k₂) are the Fourier transform coefficients of the image output, image input, and image filter impulse response respectively. Now, the filter computations become readily manageable and almost trivial. They simply involve multiplying each Fourier transform coefficient of the input image with each respective Fourier transform coefficient of the impulse response of the filter. The result is then inverse Fourier transformed back into the spacial domain as the resultant linearly filtered output image.

The transfer function furnished for the linear filtering process is given as a one dimensional equation.

Before it can be used to filter an image, however, it must be converted into two-dimensional form. It has been shown by Huang (Ref 6) that a good circularly symmetric two-dimensional linear filter can be obtained from a good one-dimensional

linear filter via the relation:

$$H(k_1, k_2) = \frac{\Lambda}{H}(\sqrt{k_1^2 + k_2^2})$$

where $^{\Lambda}$ is the one-dimensional filter impulse response at the appropriate frequency values of k_1 and k_2 . For the situation involving the previously cited 64x64 image matrices, this requires Fourier domain frequency values (k_1,k_2) , along both the real and imaginary axis, ranging from -32 cycles to +32 cycles. Due to the circular symmetry of the filter, only one 32x32 quadrant need be calculated from the equation. Once calculated, it is appropriately copied into the other three quadrants of the filter matrix. A more complete explanation of this operation appears in Appendix A.

The Question of Operating in Two Dimensions

The most obvious problem of processing in two-dimensions is simple: it takes longer, and uses more computer memory. For the one-dimensional case, the discrete Fourier transform of a sequence of N samples takes N² complex addition and multiplications; in two-dimensions, it takes N⁴ operations by brute force. For the one-dimensional case, the filtering process in the Fourier domain requires 2.N complex coefficients to be stored in computer memory; in two-dimensions 2.N² complex coefficients must be stored. To help reduce these increased requirements associated with two-dimensional processing, certain processing modifications were made.

First was the implementation of the well-known (Ref 8)

Fast Fourier Transform (FFT) technique. This reduces the number of addition and multiplications from N⁴ (64⁴=16,77,216) to 2N·Nlog₂N (128·64·6 = 49,152), a reduction of over 10 to 1. The program implementation of the FFT algorithim is via the FORTRAN subroutine called FOURT. It is a program written by Norman Brenner from the basic program by Charles Rader of MIT Lincoln Laboratory. It is a very versatile program, and offers more options than are required for the particular image processing application. But its very versatility was the reason it was selected, as it will allow calculation of odd sizes of FFT's for images other than the present 64x64 size. A more complete discussion of FOURT appears with the program listing in the appendix.

The second modification was to use disk files to store the images and complex FFT coefficients. In the existing IPS/DICOMED image processing systems each complex number occupies 4 words of storage. For one 64x64 FFT coefficient matrix to be entirely loaded into computer memory it would require 16K words. If, as in a filtering operation, two matrices were to be used at once, then 32K words would be needed; the existing minicomputer core storage is only 28K words. A technique suggested by Oppenhein (Ref 8) to reduce the requirement for two-dimensional core storage is to perform the two-dimensional FFT as a series of one-dimensional FFT's. Further, by first storing the images on random access disk files then reading in only one row or column from each appropriate disk file, the FFT operates on only those two

pieces of data at one time, and the core required to operate the program is dropped to a realizeable size. Although the processing scheme involves huge amounts of computer I/O, the time to compute and store a 64x64 point complex FFT is less than 4 minutes, and the time to accomplish filtering (matrix multiplication) is less than 2 minutes. Additionally, there is an option to have the FFT coefficients normalized by dividing all coefficients by the zero-frequency or DC term, or to have the FFT coefficients remain with their unnormalized values.

A Question of Power Spectrum Thresholding

Once the digitized image is in the Fourier domain, the calculation of the power spectrum is straight-forward. The power spectral density of an image is related to the squares of the absolute value of the Fourier coefficients and is given by:

$$\Phi(u,v) = E\left\{ \left| x(u,v) \right|^2 \right\}$$

where the expectation is over an ensemble of image transforms. The program implementation for estimating the power spectrum of a set of images is obvious from this equation, and a discussion can be found in Appendix A, Operating Procedures, 5c. The analysis program provides the capability to average up to 24 different image spectrums. These 24 images may be the same ones that are mentioned in the introduction to this paper. It is on this resultant averaged power spectrum that

the thresholding function is expected to be used.

The thresholding function was originally requested to be used with only the power spectrum. However, to provide more flexibility, it is implemented in a manner to allow its use with any specified 64x64 matrix of complex data (i.e. FFT coefficients, or power coefficients). By using the thresholding function, the analysis program user is able to interactively specify a 64x64 complex valued matrix, and to enter a real valued number against which the absolute value of every complex point is compared. The result of this thresholding operation is the creation of a 64x64 matrix which contains (in complex format) the value one for every point above the threshold and a complex zero for every point below the threshold. Both the original matrix and the threshold matrix are then available for further processing.

Since the thresholding is done in the Fourier domain, values that are linearly related (Ref 1:138-141) to spatial bandwidth (BW) and mean-square-error (MSE) are easily calculated. The BW value is simply the number of points above threshold in the Fourier domain. In the spatial domain, these above-threshold values correspond to the image pixels that would be transmitted over a digital channel with relative bandwidth BW. The MSE value is simply the sum of the power values below threshold. In the spatial domain, the MSE corresponds to the error of the image transmitted over a digital channel, with bandwidth BW described above.

The Question of Images and Image File Generation

Originally, the only requirement for image output was to generate a completely processed image ready for experimental testing. However, in an effort to make the analysis program applicable for more general use, the ability to display intermediate results is also provided. A 64x64 image file displaying the results for each of the following functional operations is prepared and stored in DICOMED/IPS format on disk: (1) the reduction of a 2048x2048 image to a 64x64 image; (2) the two-dimensional FFT calculation; (3) the power spectrum calculation; and (4) a fully processed image (either thresholded, linearly filtered, or FFT'd).

Since the images are in DICOMED/IPS format, post-processing with the IPS system is trivially implemented (Ref 7). A sample image file format appears in the appendix.

III. Laboratory Hardware and Software

The imagery equipment used for this work is located in the Avionics Laboratory on Wright-Patterson AFB, Ohio. A detailed description of the equipment is included in Reference 7. Briefly, it consists of a PDP-11/45 minicomputer with 28K of core memory and many peripherals. Included are: one RPØ3 diskpack disk drive, two RKØ5 diskcartridge disk drives, one MTU1Ø tape drive, one 132 column line printer, a Conrac video monitor, and one Tektronix 4000 series graphics terminal. Additionally, the system is interfaced to a DICOMED image scanner/recorder. With this equipment, the capability exists to perform up to a 2048x2048 point digitization of pictures. As the DICOMED digitizes the picture, it is stored on magnetic tape for follow-on processing by the PDP-11/45 Image Processing System (IPS). A description of the IPS software is also included in Reference 7.

A full description of the software written for this thesis appears in the appendix. It is written for interactive use and provides the following capabilities:

- 1. Image reduction from 2048x2048 to 64x64.
- 2. FFT of a 64x64 image.
- 3. Calculation of Φ_i (u,v) for one image, or an average $\hat{\Phi}$ (u,v) of a standard set of 24 images.
- Ability to threshold a 64x64 image as previously discussed.
- Ability to generate a 64x64 filter from a user supplied impulse response equation.

6. Inverse FFT of Fourier coefficients.

By running this program, any one of the above processes can produce an image file that is stored on the RPØ3 disk for display by the IPS system, or hardcopy picture generation by the DICOMED system.

IV. Results

Figure 1 presents some samples of output from the digital image preparation program. It should be noted that Figure 1 was generated with an arbitrary high-pass filter whose transfer function has the form:

$$H(f) = 0.5(1 + \ln(f/10 + 0.1), \text{ for } 0 \le f \le 32$$

Also note, that the slight graininess of the 64x64 pictures is due to a blow-up factor of two (4 new points for each original point). This was done solely to provide larger pictures for Figure 1.

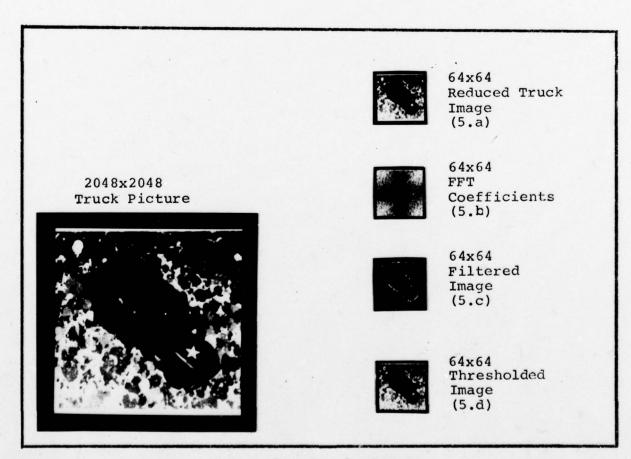


Figure 1. Sample Images

V. Summary and Recommendations

This thesis has presented a computer program to digitally process images, and in this case the processing is motivated by a desire to generate stimuli for a particular psychometric experiment. Additionally, as can be verified by reading the program description in the appendix, a general purpose routine is now made available to tailor digital processing of pictures for a large number of image filtering based applications.

Areas for future work would include modifying the program to process pictures other than the 64x64 size, and an on-line interactive tie-in between the IPS system and the processing program.

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Appendix A

User's Guide for RAZMA.TAZ

Appendix A

User's Guide for RAZMA.TAZ

Introduction

This program allows a user to perform the following functions on IPS/DICOMED images:

- A reduction of a 2048x2048 image file to a 64x64 image file.
- 2. A two-dimensional fast-fourier transform (FFT) of a 64x64 image with either normalized or unnormalized coefficients.
- Calculation of a two-dimensional power spectrum of one 64x64 image file, or the two-dimensional average power of 24, 64x64 images.
- Specification of a high-pass threshold on either the FFT file or the power file.
- 5. Generation of a two-dimensional filter (FFT domain) from a user specified impulse response equation.
- Multiplication of any threshold or filter files with any image or FFT or power files.
- Calculation of the two-dimensional inverse FFT transform on any modified FFT file.

Reference Material

1. The DOS/BATCH Handbook: Monitor Operating System

Version Ø9. Digital Equipment Corporation, Maynard,

Mass. DEC-11-ODBHA-A-D, April 1974.

2. Image Processing Software Conversion, Vol. I & II. Development Center, Air Force Systems Command, Grifiss AFB, New York 13441. February 1977. (ADA038136 & ADA038137).

Operating Procedures

This gives the ordinary routine for running RAZMA.TAZ. Specialized uses and procedures are covered under sub-heading Miscellaneous Operations.

 Program materials you will need include: User's Guide.

IPS diskcartridge (RKØ5) (AAT Lab-blue label).

"Scratch" diskcartiridge (RKØ5) (AAT Lab-#6).

ROLLIN magtape with RAZMA.TAZ program and 24 picture data sets.

IPS/DICOMED PDP-1445 computer and associated hard-ware (AAT lab).

- 2. How to 'power-up':
 - a. Place PDP-11/45 console HALT switch down, turn key of console clock-wise-to the 'on' position.
 - b. Load IPS diskpack in RKØ5 unit #Ø. Load 'scratch' diskpack in RKØ5 unit #1. Do not use 'write protect' switch. Wait until 'on-cylinder' light comes on.
 - c. Mount ROLLIN tape on tape drive. This can be omitted if program and data files are already on the scratch diskcartridge or the RPØ disk drive.
 - d. Turn on RAMTEK graphics display box.
 - e. Slowly turn on line printer, then toggle 'master clear', and toggle 'on-line' switches. This can be omitted if no printer output is expected (normally none is).

- f. Open door to RPØ disk drive to see if diskpack #1 (DOS) is installed. If not, retrieve it from the lower cabinet and install it. Turn on power switch and wait until yellow light comes on.
- g. Turn on Tektronix 4014 terminal and place it in 'local' mode. Type 'ESC' key, then ':' key. Type in that order, and only once each. This reduces the display front size. Place terminal 'on-line'.
- h. Turn on CONRAC video display.
- i. Return to the PDP-11/45 console SWR. Set in 0007768 ('one' is up) and toggle 'load ADR' switch. Set in 0007778 and toggle 'DEP' switch. Move switch from 'HALT' to 'ENABLE' and hit the 'RUN' switch.
- j. Place the thumbwheel of the AED8000 to the 'MAINTEN-ANCE' display and to ADDR CODE = 776732. Push the red IPL switch once. The LED's above the display should begin flashing. If not, go back and try again.
- k. Return to the Tektronix terminal and type RKØ: Do not type a carriage return. Enter the date and time in the format shown.
- 1. Login with \$ L0 11,11.
- m. Type \$ RUN DK1: RAZMA.TAZ, or \$ RUN DPØ: RAZMA.TAZ.
- n. Follow the yellow brick road.
- 3. How to 'power-down':
- a. To end RAZMA.TAZ, type the 'CTRL' key and the 'C' key simultaneously, followed by 'K' and 'I'. This exits to the DOS monitor. This may also be used to stop the program at any time. Next, type 'FI' to log-out from the IPS/DOS system.
- b. Place the terminal in 'LOCAL' mode, give the screen display several RESET's, and turn off the terminal.
- c. Turn off the CONRAC video monitor.
- d. Return to the PDP-11/45 console and hit the 'HALT' switch.
- e. Toggle the switches on both RKØ5 diskcartridge drives to the UNLOAD position. The doors will remain locked until the 'LOAD' light comes on. This will take about a minute. Then the cartridges can be removed.

- f. Meanwhile, the following steps may be performed.
- g. Toggle the Line printer to 'OFF LINE' and turn it off.
- h. Turn off the RAMTEK graphics display box.
- i. Push the red IPL switch on the AED8000 once. Push, then release, the yellow power switch on the RPØ disk drive. The yellow light will slowly go out. After it goes out the diskpack can be removed if desired.
- j. Unload/dismount the ROLLIN magtape, if it was loaded on the magtape drive, and turn off the magtape drive.
- k. Return to the RKØ5 diskcartridge drives and remove the diskcartridges.
- 1. Turn the key on the PDP-11-45 console fully counterclockwise to the off position.
- 4. Running the RAZMA.TAZ. The actual operation of the program is straight forward. A menu of functions is presented first and the user selects the desired function. All prompts are self-explanatory. format for all ASSIGN commands is given prior to each request for user assignment. Any error in syntax will be caught by the monitor system. However, be very careful to note the device unit number used in the command format. Failure to use the same number when typing in the command can destroy certain necessary stored program files along with the user's specified input file. Should the wrong number be typed, simply retype the command before typing 'CO'. If 'CO' has already been typed, do a 'CNTRL/C', 'KI' immediately. This closes all files and returns control to the DOS monitor. By running FILDMP or

PIP (see DOS/BATCH handbook), the user's files can be verified and/or restored. For verification of program files, see Special Procedures. After file verification or restoration, RAZMA.TAZ can be started normally.

Other than prompts and asking for file assingments there should be no other messages, except when using the FFT, POWER, and IFFT functions. In these cases, an error message will be printed about an overflow on a real to integer conversion. This is normal. It occurs during the generation of each function's image file, and refers to the DC term of the FFT coefficients. It does not affect any in ternal processing calculations. The error merely means that the value of the DC term is greater than 16,384 and exceeds the allowable 256 level gray scale of the DICOMED image processor. The DC pixel value will be zero (black pixel), in the upper left hand corner of any picture created from the image file.

Errors of any other type should not occur. If they do, it is most likely due to processing a bad data from an input file. As before, use FILDMPT or PIP to check input files for correct data.

 RAZMA.TAZ functions. This briefly describes what each function does and what files are used or generated.

- a. REDUCTION. Takes a user specified 2048x2048 image file and averages it's pixels into a 64x64 image file. The routine takes a 32x32 pixel block from the specified file and averages the entire 1024 points into one point of the 64x64 image. The output file is called AVG.IMG.
- b. FFT. Performs a two-dimensional fast fourier transform (FFT) on either a user specified image file or the AVG.IMG. file. The resultant coefficients can be either normalized (FFTCOF.NRM file) or unnormalized (FFTCOF.UNN file) as requested by the user. The routine performs the FFT by using the subroutine FOURT, first on each image row, and then on each image column. An image file of the resultant FFT coefficients is also made (FFT.IMG). The DC term is in the upper left-hand corner. This image file may be accessed in the normal manner under the IPS/DICOMED system.
- c. POWER. Uses the FFT coefficients to generate a two-dimensional power spectrum. The input file can be a single user specified FFT file, or FFTCOF. NRM, or FFTCOF.UNN. Additionally, the function will calculate the average power spectrum of the 24 storage picture coefficients. The power calculation is simply the squaring of the FFT coefficients. The resultant output file is PWRFFT.COF. An image file is also created (PWRFTT.IMG) for use on the IPS/DICOMED system.
- d. THRESHOLD. This function looks a user specified coefficient file, or PWRFFT.COF, or FFTCOF.NRM, or FFTCOF.UMM and creates a file that when used with the MULT function will pass only coefficients above a certain threshold value. This value is entered, interactively, by the user. In addition, the routine counts the number of points above the threshold and calculates a "bandwidth" number; i.e., PTS.ABOVE : 4096 = BW. Also, if the coefficients were POWER coefficients and normalized, it finds the mean-square-error of the thresholded power spectrum; i.e., the amount of power below the threshold setting. The output file contains only a mask of 1's and Ø's at the appropriate location and is called THRHLD.FIL.
- e. FILTER. This function takes a user specified filter transfer function equation and computes a two-dimensional mask file which can be used in the MULT program. The value of the mask points are based on the radial distance from the upper left-hand corner of a 32x32 square (Fig 2).

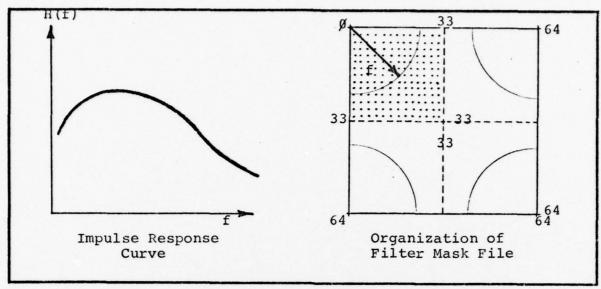
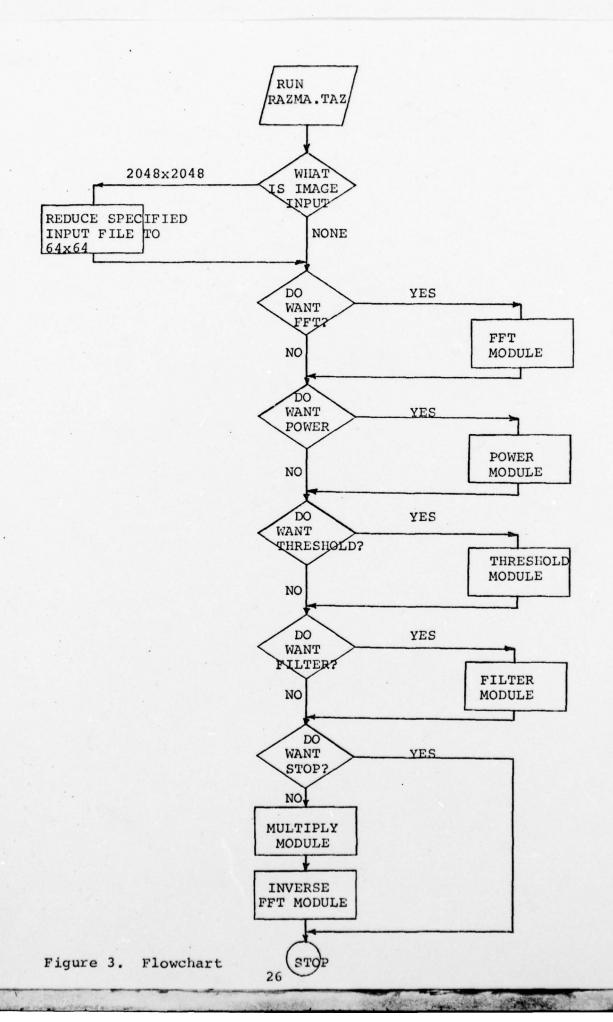


Figure 2. User Specified Filter Impulse Response

The equation is specified on line 515 of the RAZMA.TAZ program listing. To change the equation, the program must be edited and reassembled (see Miscellaneous Operations, b). The resultant output file is FILTER.COF.

- f. MULT. This functional routine takes one user specified coefficient file, or THRHOLD.COF, or FILTER. COF and multiplies it point-by-point times another user specified coefficient file, or FFTCOF.NRM, or FFTCOF.UNN, or PWRFFT.COF. It's output file is MULT.DAT.
- g. IFFT. This function performs an inverse FFT on the MULT.DAT file. The user cannot directly specify input to this file. But he can however, input indirectly. By giving the THRESHOLD function a threshold of zero, a mask of all one's will be generated. Then, using this mask with MULT and specifying the other MULT input file, the input to IFFT is assured. The output is an image file named PROCSD.IMG. As with all other image files, this is operable on the IPS/DICOMED system.
- FLOWCHART. The flowchart in Figure ³ shows the processing flow and options available in RAZMA.TAZ.



Special Procedures

- 1. NO FILE! After the \$LO and \$RUN the monitor answers with NO FILE! When this occurs, run the DOS/BATCH PIP program (see the handbook) and see if RAZMA.TAZ is on the disk you specified in the \$RUN command. If not, check the other disk. Remember, you must be logged-in under UIC=11,11. If not on either disk, use the ROLLIN tape and ROLLIN program (in handbook) to restore the RKØ5 diskcartridge on unit #1 (DK1:). Then start POWER-UP procedures
- 2. UNABLE TO OPEN FILE. This can occur any time during the running of the RAZMA.TAZ program. This usually means that an expected input file (specified by ASSIGN) or one of the 24 standard picture files does either not exist on DPØ: or two files exist with the same name. In either case, run PIP to get a listing of all files on DPØ: to see if all required files are there, and perform file manifulation as appropriate. If file cannot be found on DPØ: or DK1:, it may be necessary to ROLLIN the magtape as in the above step and start again. A minimum of the following files are required:

```
10C 13-SEP-78 (233)
10C 13-SEP-72 (233)
10C 13-SEP-72 (233)
10C 13-SEP-78 (233)
DIRECTORY DK12 E 11,11 3
15-SEP-78
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               APC1
APC2
APC3
                                                                                                                                                        640 13-5EP-78 (233)
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ARTY2 .COF
ARTY3 .COF
ARTY4 .COF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                . TMG
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CURTK1. IMG
CURTK2. IMG
                                                                 .COF
.COF
.COF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CURTK3. ING
CURTK4. ING
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     10C 13-SEP-78
CURTKI . COF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             OPHTKE. IMG
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       OPHTK2.IMG
OPHTK4.IMG
OPHTK4.IMG
SHER1 IMG
SHER2 IMG
SHER2 IMG
SHER4 IMG
MEGGA1 IMG
MEGGA1 IMG
MEGGA3 IMG
MEGGA4 IMG
MEGG
CURTK4.COF
                                                                                                                                                            64C 13-SEP-78 (233)
64C 13-SEP-78 (233)
OPNTK2.COF
                                                                                                                                                          640 13-5EP-78 (233)
OPNTK4.COF
SHER1 .COF
SHER2 .COF
SHER3 .COF
SHER4 .COF
M60A1 .COF
M60A2 .COF
                                                                                                                                                          640
640
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                                                                                                                                                            64C 13-5EP-78
64C 13-5EP-78
64C 13-5EP-78
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64C 13-5EP-78
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RAZMA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      15-SEP-78
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(833)
(833)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         TOTL BLKS1
                                                                 .COF
```

- 3. EXPONENT OVERFLOW or OVERFLOW DURING REAL TO INTEGER CONVERSION. This can occur during the operation of all functions except FILTERING or THRESHOLDING. It is the result of processing with invalid data in the assigned input files, or bad data from one of the 24 stored image files. In either case, the contents of files can be inspected using the DOS/BATCH program FILDMP (see handbook). The organization and contents of typical image and coefficient files are shown in Appendix C. If bad data is suspected in any of the 24 noted image files, the best procedure is to use the DOS/BATCH program PIP to restore the files; an example of how to do this is shown in the next section.
- 4. UNABLE TO READ SPECIFIED FILE FORMAT or END OF FILE-END OF MEDIUM. This occurs when the RAZMA.TAZ program encounters files with improper file organization or length. Again, as above, use FILDMP or PIP to verify and transfer files.

Miscellaneous Operations

- 1. Generating Files. There are three catagories of files associated with the RAZMA.TAZ program.
- a. Programming operating files. These are files generated by the program for it's own use. A discussion of these files is found in the comments of the program listing.
- b. Twenty-four standard picture file sets. Each picture set consists of an image file and a normalized FFT coefficient file. These picture sets have already been generated and are stored for use by the program in the POWER function. A copy of these files is on the ROLLIN magtape.
- c. User impact files. These are files specified by the user with the ASSIGN command. The file will be either the image or the FFT coefficient type.

The origin of the image files can be from the IPS/DICOMED system (2048x2048 or 64x64) or the RAZMA.TAZ program (64x64). Directions for creating image files under the IPS/DICOMED system can be found in Volume 1 of Reference 2. Creating a 64x64 image file under RAZMA.TAZ can be accomplished by using the reduction function, and then exiting to use PIP to rename the newly generated AVG.IMG file to whatever name the user desires. To save these files on magtape, PIP and ROLLIN are used. For

each file, the PIP command is: #DK1: name.extn/CO < DPØ: name.extn. Then, ROLLIN is used (DOS/BATCH handbook) to copy DK1: and create a new ROLLIN tape.

The origin of the FFT coefficient files must be from running RAZMA.TAZ. The file is simply created by running the FFT function, and then exiting to use PIP to rename the newly created FFTCOF.NRM or FFTCOF.UNN file to whatever name the user desires. The file can then be saved in the same manner as the image files.

- 2. Restoring files. For RAZMA.TAZ to operate, all files must be on DPØ:. If they are not (a minimum listing appears in Special Procedures), or for some reasons the files become invalid, the files must be restored. A permanent copy of all files is on the ROLLIN magtape. This tape can be loaded onto DKl: (DOS/BATCH handbook), and then the appropriate file transferred under PIP to DPØ:. The proper PIP command is: #DPØ: name.extn/CO CDKl: name.extn.
- 3. Changing RAZMA.TAZ. Best advice: DON'T. However, for the brave and/or foolhardy, a bubble chart and program listing is given in Appendix B. Once the changes have been made under EDIT (see handbook), the proper Fortran assembly must be made. The proper command after \$RUN FORTRAN is: #DK1: RAZMA, LP: < DK1: edit file name. extn / ON; or, #DPØ: RAZMA, LP: < DK1: edit file name. extn/ON. (Assuming EDIT was done on DK1:). This is important because RAZMA.TAZ uses single word integer variables. When the assembly is done, the linker command after \$RUN LINK is: #DK1: RAZMA.TAZ < DK1: RAZMA/CC, DKØ: FTNLIB/L/E; or: #DPØ: RAZMA.TAZ < DK1: RAZMA/CC, DKØ: FTNLIB/L/E as appropriate.

User's Guide

Sample Sessions

EDIT

FORTRAN

PIP

ROLLIN

RAZMA.TAZ

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EDIT U07-03
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#THELERABMA.FIN<DKIERAZMA.FIN

TROOPE

DATA(N)=0.5*(1.0+ALOG(RADIAL*0.1+1.0))

DATA(N) = 0.5*(1.0+ALOG(RADIAL*0.1+1.0))
CONTINUE DATA(N)=0.5*(1.0+ALOG(RADIAL*0.1+1.0)) и ж и и ж ж и т н и и и о д и о и и д и

DATA(N)=0.5*(1.0+ALOG(RADIAL*0.1+1.0)) CONTINUE

SAU PORTRN FORTRON UGS.13 FORTRANA, LPAKDK14RAZMA.FTN/ON

SRU LINK

17

LIMK VO1-04 #DK1±RAZMA.TAZKDK1¢RAZMA/CC,DK0¢FTNLIB/L/E

SPACE USED 030420, SPACE FREE 061132 4.0 .KI

A- RENAMING FILE & STORING FILE -3- RESTORING FILE #RU PIP PIP VIO-02 #INSTITER.ING/COKDPO\$PROCSD.IMG #EPO#FILTER.IMG/CO<DK1#FILTER.IMG

(0

#PK12FILTER.IMG/DI

DK13

E 11,11 3

FILTER.IMG 100 15-SEP-78 <233>

#DROSFILTER.ING/DI

DPOT

E 11,11 3

FILTER.IMG SC 15-SEP-78 (233)

**C

ROLLEN UB7

6

0

0

#:TOMRAMAKDKIM/RW/DATEM13-SEP-78 #:TOMRAMAKDKIM/DATEM13-SEP-78

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ON NACTAPE

FOLLIN UB?

#IK1# CMT0#RAZMA/FI

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FURNISHED TO CONTINUE. MULTIPLYING MACHALLITHINK YOU CAN FOOL MOTHER NATURE EHM FOOE MULT TYPE C TO CONTINUE, TYPE S TO STOP THPESHOLD WORKING END THRESHOLD IFFT WORLING THE POLICE BANGE ON REAL TO INTEGER CONJERSION \$ THEY WORLD SE9 MAIN. COLTS THE INPUT IMAGE FILE DUST BE SPECIFIED.

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AND SOURCE SOURCE.

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SAS DPOXCURTERING, 7 N FOR NOPMALIZED FFT COEFF U FOR UNNORMALIZED COEFF TYPES B FOR BIGGIE /20482048/ J FOR JUNIOR /64264/ S FOR STANDARD SET OF 24 N FOR HONE SPEAK TO ME ABOUT IMAGE INPUT SPU DKIAFAZNA.TAZ TYPET

DONE POWER

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N

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TYPE P FOR POWER, F FOR FILTER, T FOR THRESHOLD P

TYPE C TO CONTINUE, TYPE S TO STOP

TYPES U FOR UNNILLA PLAIM FFT COEFF
A FOR AUERAGED/SOUNDED FFT INDUT
A
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THE FORM - 0.0000 /UP TO 1% THAILING DIGIPS/

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THE INPUT IMMGE FILE NUST BE SPECIFIED.

IF NOT MET HSSIGNED, PLEASE DO SO NOW, THE FORM ISA

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THEN TYPE OD TO CONTINUE.

\$45 DPOINTNE.EXT, 7

\$45 DPOINTNE.EXT, 7

\$60

TYPES B FOP RIGGIE /204822048.
J FOR JUNIOR /64564/
S FOR STANDARD SET OF 24
N FOR HOME

SPEETINGS AND SOLUTIONS SPEAK TO ME ABOUT IMAGE INPUT

SPU DKISPHERN.TRE

N FOR NORMALIZED FFT COEFF U FOR UNIVERNALIZED COEFF TYPET

FFT UCPYING

FORTBOSGER REAL OUTSIDE PANGE ON FEAL TO INTEGER CONVERSION NAME SEC MAIN. CO179

TYPE C TO CONTINUE, TYPE S TO STOP

TYPE P FOP POWER, F FOR FILTEP, T FOR THRESHOLD

TAPE N TO MAKE NEW THRESHOLD FILE, TAPE O TO USE OLD FILE

THE OLD THRESHOLD FILE MUST RE SPECIFIED.

IF ALREALY MASIGNED, TYPE CO TO CONTINUE.

FOR THE ASSIGNED, PLEMSE DO SO NOW. THE FORM ISA

MASS DOCUMENTAL.

THEN TYPE CO TO CONTINUE.

AND SPORTH LD.FIL,1

\$60

IF FFT COEFF WERE JUST NOW MADE, THE FILE IS ALREADY ASSIGNED. TYPE CO TO CONTINUE.

IF NOT YET ASSIGNED, PLEMSE DO SO NOW. THE FORM ISA BAS DROADMINE.EXT.3

THEN TYPE CO TO CONTINUE.

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36

DONE FFT

DONE MULT

IFFT WORKING DOME IFFT &

THE IMPUT IMAGE FILE MUST BE SPECIFIED.

IF NOT MET ASSIGNED, FLEMSE DO SO MOM, THE FORM ISA

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THEN TYPE OF TO CONTINCE.

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SAS DROAC WRITHING, 7

TYPES B FOR PIGGIE /204822048/ J FOR JUNIOR /64364/ S FOR STRUBHRD SET OF 24 N FOR NOWE

SPEAK TO ME ABOUT INAGE INPUT

SPU DK1±PAEMA.TAZ

N FOR NORMALIZED FFT COEFF U FOR UNNORMALIZED COEFF TYPET

FORTBOBGES REAL CUTSIDE PAMOE ON PEAL TO INTEGER COMPERSION NAME SEGMAIN. COLTS FFT WORKING

TYPE P FOR POWER, F FOR FILTER, T FOR THRESHOLD F TYPE C TO CONTINUE, TYPE S TO STOP

C TO USE CURPENT FILTEP EQUATION FOR FILE O TO USE AN OLD FILTEP FILE TYPER

MAKING FILTER DONE FILTER

TYPE C TO CONTINUE, TYPE S TO STOP

IF FFT COEFF UEPE JUST NOW MADE, THE FILE IS ALREADY ASSIGNED. TYPE CO TO CONTINUE. IF NOT MET ASSIGNED, PLEMSE DO SO NAW. THE FORM ISS SAS DPOSNAME.ENT 3 THEN TYPE CO TO CONTINUE. ACOS DEOSCO.

Politiplicing to can fool hother bating sa-

DONE FFT

User's Guide
Program Bubble Chart
Program Listing

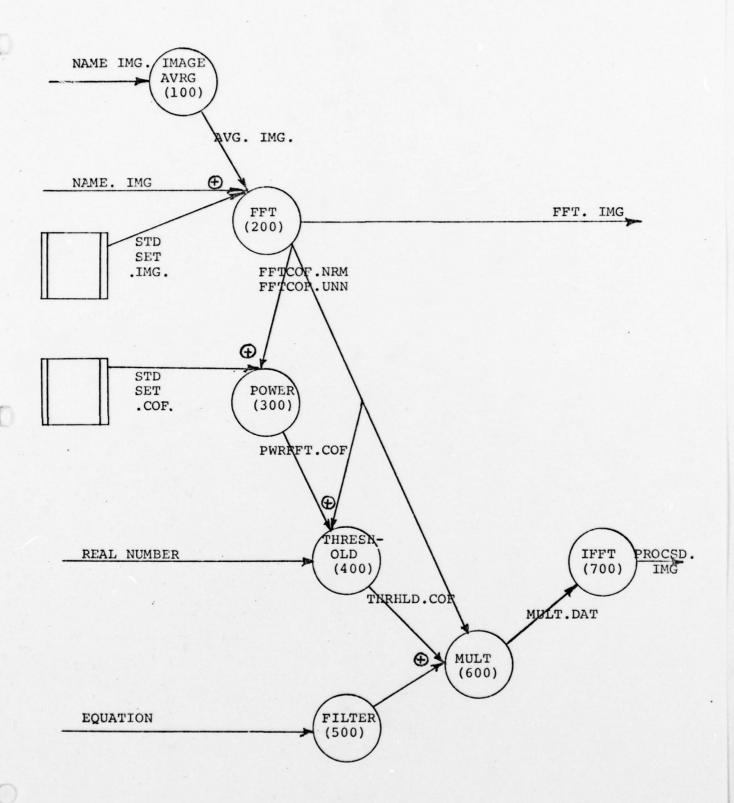


Figure 4. Program Bubble Chart

ASSESSED FOR THE PROPERTY OF T

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************
               PROGRAM RAZMA, TAZ
      **********************
      THIS PROGRAM HAS THE FOLLOWING DISK (DPØ1) RANDOM ACCESS FILE
      ASSIGNMENTS:
           .IMG - OUTPUT OF REDUCE, INPUT TO FFT
      SCRATC.DAT - USED IN FFT
      FFTCOF NRM - OUTPUT OF FFT, INPUT TO POWER
      (FFTCOF. UNN)
                            INPUT TO THRESHOLD
                            INPUT TO MULT
C
```

. IMG - OUTPUT OF FFT INPUT TO POWER PWRFFT, COF . OUTPUT OF POWER, INPUT TO THRESHOLD PWRFFT, IMG - OUTPUT OF POWER THRHLD, FIL . OUTPUT OF THRESHOLD, INPUT TO MULT FILTER, COF - OUTPUT OF FILTER, INPUT TO MULT MULT .DAT . OUTPUT OF MULT, USED IN IFFT PROCED, IMG . OUTPUT OF IFFT

THE FOLLOWING DEVICES ARE INTERACTIVELY ASSIGNED TO THESE FILES DURING THE RUNNING OF THE INDICATED MODULES:

FILE 2 3 1 4 . IMG BIG REDUCE . IMG AVG FFT FFTCOF. ---MULT THRES POWER POWFFT COF THRES FILTER, COP MULT THRHLD.COF MULT

ANY I/O REFERENCE MADE TO DEVICE NUMBERS AFTER THE DEVICES HAVE BEEN INTERACTIVELY ASSIGNED DURING THE MODULES SPECIFIED ABOVE. WILL OPERATE ON THE FILE DATA EQUATED WITH THAT DEVICE NUMBER.

COMPLEX DATA(64), DATBUF(64), DCVAL, NOFILS, MSE BYTE HEADER(64,8), BUFFER(2048), BBUF(2), BCOL(128), NULLS(64,8) INTEGER INPTR, AVGPTR, DATSPT, DATSPT, FFTPTR, DATSPT, DATBPT INTEGER SUM, BUF, OFFSET, COL (64), UNIT, COFPTR, COFING, AVGFFT INTEGER THRSPT, OUTBW, BW, IERR, DAT1PT, DAT5PT, DAT4PT, ASGD7, PWRON EQUIVALENCE (BCOL(1), COL(1)), (BBUF(1), BUF) DATA HEADER/0,0,79,58,64,0,64,505+0/ DATA NULL8/512*0/

WRITE (6.5) WRITE (6,6) WRITE (6,11) WRITE (6,7) 2 WRITE (6,8)

1

CCC

C

•

DEFINE FILE 7(4097,512,U,INPTR)

17152156

15-SEP-78

PAGE

2

RAN V06.13

```
RAN V06.13
                              17152156
                                           15-SEP-78
                                                        PAGE
                                                                 3
             CALL SETFIL(8, 'AVG, IMG', IERR, 'DP', 0)
             DEFINE FILE 8(80,32,U,AVGPTR)
,
             WRITE (6,110)
     110
             FORMAT( AVERAGE WORKING )
             INPTR=2
             AVGPTR=1
             DO 115 J#1,8
             WRITE (8°AVGPTR) (HEADER(I,J), I=1,64)
     115
             DO 116 J=1.8
             WRITE (8°AVGPTR) (NULLS(I, J), I=1,64)
     116
             DO 170 I=1,64
               DO 120 K=1,64
     120
               COL(K)=Ø
               00 150 J=1,32
               READ (7ºINPTR) (BUFFER(N), N=1, 1024)
               READ (7"INPTR) (BUFFER(N), N=1025, 2048)
                 DO 140 K=1,64
                 OFFSET#(K=1)+32
                 SUM=0
                    DO 130 L=1,32
                    INDX=L+OFFSET
                    BBUF(1) = BUFFER(INDX)
                    SUM=SUM+BUF
                    CONTINUE
     130
                  COL(K) #SUM/32+COL(K)
     140
                  CONTINUE
     150
               CONTINUE
               DO 160 K#1,64
               COL(K)=COL(K)/32
     160
               CONTINUE
             WRITE (8"AVGPTR) (BCOL(N), N#1, 128, 2)
             CONTINUE
     170
             ENDFILE 7
             ENDFILE 8
             WRITE (6, 195)
     190
             WRITE (6,11)
     192
             WRITE (6,196)
             WRITE (6,11)
     195
             FORMAT( DONE IMAGE AVERAGING )
             FORMAT( TYPE C TO CONTINUE, TYPE S TO STOP ')
     196
             READ (6,12) INCS
             IF (INCS, EQ, 1HS) GOTO 900
             IF (INCS. NE. 1HC) GOTO 192
             GOTO 38
             **** FFT MODULE ****
     200
             CALL SETFIL(8, 'AVG, IMG', IERR, 'DP', 0)
             DEFINE FILE 8(80,32,U,AVGPTR)
             IF (ASGD7.EG. 1HY) GOTO 215
             WRITE (6,205)
             WRITE (6,207)
             WRITE (6,208)
             WRITE (6,209)
     205
             FORMAT( THE INPUT IMAGE FILE MUST BE SPECIFIED. ')
             FORMAT(" IF NOT YET ASSIGNED, PLEASE DO SO NOW, THE FORM IS: ")
     207
```

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PAGE
RAN VØ6.13
                               17:52:56
                                            15-SEP-78
             FORMAT ( SAS DPO : NAME , EXT, 7 )
    208
             FORMAT ( THEN TYPE CO TO CONTINUE. ")
    209
             PAUSE
             DEFINE FILE 7(80, 32, U, AVGPTR)
    210
             WRITE (6,215)
             WRITE (6,216)
             WRITE (6,11)
             FORMAT ( TYPE :
                               N FOR NORMALIZED FFT COEFF ")
    215
                               U FOR UNNORMALIZED COEFF ")
    216
             FORMAT(
             READ (6,12) NORMUN
             DEFINE FILE 3(64,256,U,DAT3PT)
             CALL SETFIL (3, "SCRATC, DAT", IERR, "DP", 0)
             DEFINE FILE 2(64,256,U,DAT2PT)
             IF (NORMUN, EG. 1HN) CALL SETFIL (2, "FFTCOF, NRM", IERR, "DP", 0)
             IF (NORMUN, EQ. 1HU) CALL SETFIL (2, "FFTCOF, UNN", IERR, "DP", 0)
             IF (NORMUN, NE, 1HU, AND, NORMUN, NE, 1HN) GOTO 210
             DEFINE FILE 1(80, 32, U, FFTPTR)
    217
             CALL SETFIL(1, "FFT, IMG", IERR, "DP", 0)
             WRITE (6,219)
             FORMAT ( * FFT WORKING ')
    219
             AVGPTR=17
             DAT2PT=1
             DAT3PT=1
             FFTPTR=1
             SCALE=1.0/64.0
             DO 220 J#1,8
    220
             WRITE (1°FFTPTR) (HEADER(I,J), I=1,64)
             DO 225 J=1.8
     225
             WRITE (1°FFTPTR) (NULLS(I,J), I=1,64)
             DO 238 K=1,64
     230
             COL(K)=0
             DO 250 I=1,64
              IF(ASGD7, EQ. 1HY) READ(8'AVGPTR) (BCOL(N), N=1, 128, 2)
             IF (ASGD7. NE. 1HY) READ (7"AVGPTR) (BCOL(N), N=1, 128, 2)
                DO 240
                       J=1.64
                DATA(J) = COL(J)
     240
                CONTINUE
              CALL FOURT (DATA, 64, 1, -1, 1, 0)
              WRITE (3°DAT3PT) (DATA(N), N=1,64)
     250
              CONTINUE
             DO 290 K=1,64
              DATSPT#1
                DO 260 I=1,64
                READ (3 DATSPT) (DATBUF(N), N=1,64)
                DATA(I) #DATBUF(K)
                CONTINUE
     260
              CALL FOURT (DATA, 64, 1, -1, 1, 0)
              IF (NORMUN, EQ, IHU) GOTO 270
              SCALE#256.0+64.0
              J=1
              IF(K=1) 265,265,266
     265
              DCVAL=DATA(1)
              J=J+1
                DO 267 I=J,64
     266
                DATA(I) #DATA(I)/DCVAL
```

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RAN VØ6,13
               CONTINUE
    267
    270
             WRITE (2°DAT2PT) (DATA(N), N=1,64)
               DO 280 I=1,64
               COL(I)=(CABS(DATA(I)))*SCALE
    280
               CONTINUE
             WRITE (1"FFTPTR) (BCOL(N), N=1,128,2)
    290
             CONTINUE
             ENDFILE 1
             ENDFILE 2
             ENDFILE 3
             ENDFILE 7
             ENDFILE 8
             WRITE (6,296)
             WRITE (6,11)
    295
             WRITE (6,297)
             WRITE (6,11)
    296
             FORMAT( DONE FFT )
    297
             FORMAT( TYPE C TO CONTINUE, TYPE S TO STOP ')
             READ (6,12) INCS
             IF(INCS, EQ. 1HS) GOTO 900
             IF (INCS.NE. 1HC) GOTO 295
    298
             WRITE (6,299)
             WRITE (6,11)
    299
             FORMAT( TYPE P FOR POWER, F FOR FILTER, T FOR THRESHOLD )
             READ (6,12) IPFT
             IF(IPFT.EG. 1HF) GOTO 500
             IF (IPFT.EQ. 1HT) GOTO 400
             IF (IPFT. NE. 1HP) GOTO 298
             GOTO 300
             **** POWER MODULE ****
    300
             CALL SETFIL (8, "PWRFFT. IMG", IERR, "DP", 0)
             DEFINE FILE 8(80,32,U,DATBPT)
             DATSPT=1
             DO 301 J=1,8
             WRITE(8ºDAT8PT) (HEADER(I, J), I=1,64)
    301
             DO 302 J=1,8
    302
             WRITE(8 DATBPT) (NULLS(I, J), I=1,64)
    303
             WRITE(6, 304)
             WRITE (6,11)
    304
             FORMAT(" TYPE: 0, FOR ONLY ONE FFT INPUT: S, FOR STD 24 FFT COEFF ")
             READ (6,12) INOS
             PWRONE Y
             IF(INOS, EQ, 1HS) GOTO 312
             IF (INOS, NE, 1HO) GOTO 303
             IF (NORMUN, EQ. 1HN) CALL SETFIL (5, "FFTCOF, NRM", IERR, "DP", 0)
             IF (NORMUN, EQ. 1HU) CALL SETFIL (5, "FFTCOF, UNN", IERR, "OP", 0)
             IF (NORMUN, EQ. 1HN, OR, NORMUN, EQ. 1HU) GOTO 308
             WRITE (6,305)
             WRITE (6, 306)
             WRITE (6,307)
             FORMAT( FFT INPUT MUST BE SPECIFIED.
                                                      PLEASE DO SO NOW. ")
    305
             FORMAT( THE FORM IS:
    306
                                         SAS DPØ: NAME. EXT, 5 ")
    307
             FORMAT( THEN TYPE CO TO CONTINUE. ")
             PAUSE
    308
             DEFINE FILE 5(64, 256, U, DATSPT)
```

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             CALL SETFIL(1, "PWRFFT, COF", IERR, "DP", 0)
             DEFINE FILE 1(64,256,U,DAT1PT)
             WRITE (6,309)
    309
             FORMAT( SQUARING FFT/S/ )
             DAT1PT=1
             DATSPT#1
             DO 311 I=1,64
             READ (5"DATSPT) (DATA(N), N=1,64)
               DO 310 J=1,64
               DATA(J) = DATA(J) * DATA(J)
               COL(J)=(CABS(DATA(J)))
    310
               CONTINUE
             WRITE (1"DAT1PT) (DATA(N), N=1,64)
             WRITE(8'DAT8PT) (BCOL(N), N=1, 128, 2)
    311
             CONTINUE
             ENDFILE 1
             ENDFILE 5
             ENDFILE 8
             GOTO 390
             WRITE (6,309)
    312
             CALL SETFIL (5, "PWRFFT, COF", IERR, "DP", 0)
             DEFINE FILE 5(64,256, U, DATSPT)
             SCALE=64.0**3
             NOFILS=(24.0,24.0)
             DO 313 I=1,64
             DATBUF(I)=(0.0,0.0)
             CONTINUE
    313
             DATSPT=1
             DO 314 I=1,64
             WRITE (5 DATSPT) (DATBUF(N), N=1,64)
             CONTINUE
    314
             UNIT=5
             DO 360
                     I=1,24
             DATSPT=1
             COPPTR#1
             IF(UNIT+4) 319,315,317
    315
               DO 316 J=1,4
               ENDFILE J
    316
    317
               DO 318 J=1,4
               DEFINE FILE J(64, 256, U, COFPTR)
    318
             UNITED
    319
             UNIT=UNIT+1
    320
             IF(I=1) 322,321,322
             CALL SETFIL(1, 'APC1, COF', IERR, 'DP', 0)
    321
             CALL SETFIL (2, "APC2, COF", IERR, "DP", 0)
             CALL SETFIL(3, "APC3, COF", IERR, "DP", 0)
             CALL SETFIL (4, "APC4. COF", IERR, "DP", 0)
    322
             IF(I=5) 335,323,324
    323
             CALL SETFIL(1, "ARTY1.COF", IERR, "DP", Ø)
             CALL SETFIL(2, 'ARTY2, COF', IERR, 'DP', 0)
             CALL SETFIL (3, "ARTY3, COF", IERR, "DP", 0)
             CALL SETFIL (4, "ARTY4, COF", IERR, "DP", 0)
    324
             IF(I=9) 335,325,326
    325
             CALL SETFIL(1, "CVRTK1, COF", IERR, "DP", 0)
             CALL SETFIL(2, CVRTK2, COF', IERR, 'DP', 0)
```

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                                                                   7
             CALL SETFIL (3, "CVRTK3, COF", IERR, "DP", 0)
             CALL SETFIL (4, CVRTK4, COF*, IERR, DP*, 0)
             IF(I=13) 335,327,328
    326
             CALL SETFIL(1, "OPNTK1.COF", IERR, "DP", Ø)
    327
             CALL SETFIL(2, "OPNTK2, COF", IERR, "DP", 0)
             CALL SETFIL (3, "OPNTK3, COF", IERR, "DP", 0)
             CALL SETFIL (4, "OPNTK4, COF", IERR, "DP", 0)
    328
             IF(I=17) 335,329,330
    329
             CALL SETFIL(1, "M60A1, COF", IERR, "DP", 0)
             CALL SETFIL(2, "M60A2, COF", IERR, "DP", 0)
             CALL SETFIL (3, "M6@A3, COF", IERR, "DP", @)
             CALL SETFIL (4, "M60A4, COF", IERR, 'DP", 0)
             IF(1-21) 335,331,335
    330
             CALL SETFIL(1, 'SHER1, COF', IERR, 'DP', 0)
    331
             CALL SETFIL(2, 'SHER2, COF', IERR, 'DP', 0)
             CALL SETFIL (3, "SHER3, COF", IERR, "DP", 0)
             CALL SETFIL (4, "SHER4. COF", IERR, "DP", 0)
    335
             CONTINUE
               00 350 J=1,64
               READ(5°DATSPT) (DATBUF(N), N=1,64)
               READ(UNIT*COFPTR) (DATA(N), N=1,64)
                 DO 337 K=1,64
    337
                 DATA(K)=DATA(K) *DATA(K)
                 DO 340 K=1,64
                 DATBUF(K) = DATBUF(K) + DATA(K)
    340
                 CONTINUE
               DATSPT=DATSPT=1
               WRITE(5*DAT5PT) (DATBUF(N), N=1,64)
    350
               CONTINUE
             CONTINUE
    360
    365
             DATSPT=1
             DO 380 I=1,64
             READ(5°DATSPT) (DATA(N), N=1,64)
               DO 370 J=1,64
               DATA(J)=DATA(J)/NOFILS
               COL(J) = (CABS(DATA(J))) * SCALE
    370
               CONTINUE
             DATSPT=DATSPT=1
             WRITE(5°DATSPT) (DATA(N), N=1,64)
             WRITE(8 DATEPT) (BCOL(N), N=1, 128, 2)
    380
             CONTINUE
             DO 385 I=1,5
             ENDFILE I
    385
             ENDFILE 8
    390
             WRITE (6,395)
             WRITE (6,11)
             FORMAT( DONE POWER )
    395
             GOTO 400
    C
             ***** THRESHOLD MODULE ****
             WRITE (6, 405)
    400
             WRITE(6,11)
    405
             FORMAT( TYPE N TO MAKE NEW THRESHOLD FILE, TYPE O TO USE OLD FILE ")
             READ (6, 12) INNO
             IF (INNO.EQ. 1HO) GOTO 600
             IF (INNO. NE. 1HN) GOTO 400
```

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    410
             WRITE (6,415)
             WRITE (6,416)
             WRITE (6,11)
    415
             FORMAT( TYPE: V FOR VANILLA PLAIN FFT COEFF ")
                               A FOR AVERAGED/SQUARED FFT INPUT *)
    416
             FORMAT ( *
             READ (6, 12) INVA
             IF(INVA, EQ. 1HA) CALL SETFIL(4, *PWRFFT, COF*, IERR, *DP*, Ø)
             IF (INVA, EQ. 1HY, AND, NORMUN, EQ. 1HN)
             1CALL SETFIL (4, "FFTCOF, NRM", IERR, "DP", 0)
             IF (INVA, EQ, 1HV, AND, NORMUN, EQ, 1HU)
             1CALL SETFIL (4, "FFTCOF, UNN", IERR, "DP", 0)
             IF (INVA. NE. 1HA. AND. INVA. NE. 1HV) GOTO 410
             IF (NORMUN, EQ. 1HN, OR, NORMUN, EQ. 1HU, OR, PWRON, EQ. 1HY) GOTO 430
             WRITE (6,424)
             WRITE (6, 425)
             WRITE (6, 426)
             WRITE (6,427)
             WRITE (6,428)
             FORMAT( THE FILE TO BE THRESHOLDED MUST BE SPECIFIED. ")
    424
             FORMAT ( IF NOT YET ASSIGNED, PLEASE DO SO NOW. 1)
    425
             FORMAT ( THE FORM IS: ")
    426
             FORMAT( SAS DPO: NAME, EXT, 4 ")
    427
    428
             FORMAT(" THEN TYPE CO TO CONTINUE ")
             PAUSE
    430
             DEFINE FILE 4(64,256,U,DAT4PT)
             CALL SETFIL(1, "THRHLD.FIL", IERR, "DP", Ø)
             DEFINE FILE 1(64,256, U, THRSPT)
             WRITE (6,431)
    432
             WRITE (6,433)
             WRITE (6,11)
             FORMAT(" SPECIFY A REAL VALUE FOR THE THRESHOLD OF ")
    431
             FORMAT( THE FORM = 0.0000 /UP TO 15 TRAILING DIGITS/ 1)
    433
             READ (6,435, ERR=432) THRES
    435
             FORMAT (F18, 15)
             WRITE (6, 439)
             WRITE (6,11)
             FORMAT( THRESHOLD WORKING )
    439
             DAT4PT=1
             THRSPT=1
             BW=Ø
             MSE=(0.0,0.0)
             DO 470 I=1,64
             READ (4°DAT4PT) (DATA(N), N=1,64)
               DO 460 J=1,64
               DATBUF (J) = (1,0,0,0)
               BELOW=CABS(DATA(J))=THRES
    450
               IF (BELOW) 451,453,453
    451
               MSE=MSE+DATA(J)
               OUTBW=OUTBW+1
               DATBUF(J) = (0.0,0.0)
    453
               CONTINUE
    460
               CONTINUE
             WRITE(1"THRSPT) (DATBUF(N), N=1,64)
    470
             CONTINUE
             ENDFILE 1
```

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```
ENDFILE 4
        BW=4096-OUTBW
        ABSMSE=CABS(MSE)
        FRACBW=FLOAT(BW)/4096.0
        WRITE(6, 480) THRES
        WRITE (6,482) ABSMSE
        WRITE (6,484) BW, FRACBW
        WRITE (6,11)
480
        FORMAT( THIS THRHLD FIL USED A REAL THRESHOLD OF ",F18.15)
        FORMAT( THE ABSOLUTE MSE WAS = ",F18,15)
482
484
        FORMAT( AND THE BANDWIDTH WAS= 1,14,1/4096 OR 1,F12,9)
490
        WRITE (6,495)
        WRITE (6,11)
491
        WRITE (6,496)
        WRITE (6,11)
495
        FORMAT ( END THRESHOLD )
496
        FORMAT( TYPE C TO CONTINUE, TYPE S TO STOP ")
        READ (6,12) INCS
        IF (INCS.EG. 1HS) GOTO 900
        IF (INCS. NE. 1HC) GOTO 491
        GOTO 600
        **** FILTER MODULE ****
500
        WRITE (6,505)
        WRITE (6,506)
        WRITE (6,11)
                         C TO USE CURRENT FILTER EQUATION FOR FILE ")
505
        FORMAT( TYPE:
        FORMAT ( *
506
                         O TO USE AN OLD FILTER FILE ").
        READ (6,12) INCO
        IF (INCO, EQ. 1HO) GOTO 600
        IF (INCO, NE, 1HC) GOTO 500
510
        WRITE (6,512)
512
        FORMAT ( MAKING FILTER ")
        DEFINE FILE 1(64,256, U, DAT1PT)
        CALL SETFIL(1, "FILTER, COF", IERR, "DP", 0)
        KAPA1=0
        KAPA2=0
        SIGMA1=0.
        SIGMA2=0.
        DAT1PT=1
        IFOLD=34
        DO 530 M=1,64
        MEMM
          DO 520 N=1,64
          NNEN
          IF (M. GE. IFOLD) MM=66+M
          I=MM=1
          IF (N. GE. IFOLD) NN=66=N
          J=NN-1
          SQIJ=1**2+J**2
          RADIAL=SQRT(SQIJ)
515
          DATA(N)=0.5*(1.0+ALOG(RADIAL*0.1+1.0))
520
          CONTINUE
        WRITE (1"DAT1PT) (DATA(N), N=1,64)
530
        CONTINUE
```

WRITE (6,645)

DAT1PT=1

645

FORMAT(MULTIPLYING)

```
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                                                                11
             DAT2PT=1
             DAT3PT=1
             DO 680 I=1,64
             READ (3°DAT3PT) (DATA(N), N=1,64)
             READ (1'DAT1PT) (DATBUF(N), N=1,64)
             IF (NORMUN. EQ. 1HU) GOTO 665
             K=1
             IF(1-1) 650,650,655
             WRITE (6,651)
     650
             FORMAT( AH-HA..., THINK YOU CAN FOOL MOTHER NATURE EH! ")
     651
             DCVAL=DATA(1)
              K=K+1
                DO 660 J=K,64
     655
                DATA(J)=DATA(J)*DCVAL
                CONTINUE
     660
     665
                DO 670 J=1,64
                DATA(J) = DATA(J) * DATBUF(J)
     670
                CONTINUE
              WRITE (2°DAT2PT) (DATA(N), N=1,64)
     680
             CONTINUE
             ENDFILE 1
              ENDFILE
             ENDFILE 3
              WRITE (6,695)
              WRITE (6,11)
             FORMAT ( DONE MULT ")
     695
             GOTO 700
              **** INVERSE FFT MODULE ****
     700
5
              CALL SETFIL(2, "MULT, DAT", IERR, "DP", 0)
              DEFINE FILE 2(64, 256, U, DATZPT)
              CALL SETFIL (8, *PROCSD, IMG*, IERR, *DP*, 0)
3
              DEFINE FILE 8(80,32, U, DATEPT)
              WRITE (6,730)
              FORMAT ( * IFFT WORKING *)
     730
              DAT2PT=1
              DATSPT=1
              SCALE=1.0/4096.0
              DO 740 J=1,8
              WRITE (8°DAT8PT) (HEADER(I, J), I=1,64)
     740
              CONTINUE
              DO 745 J=1,8
              WRITE (8 DATEPT) (NULLS(I, J), I=1,64)
7
     745
              CONTINUE
3
              DO 750 I=1,64
              READ (2°DAT2PT) (DATA(N), N=1,64)
              CALL FOURT (DATA, 64, 1, 1, 1, 0)
              DAT2PT=DAT2PT=1
              WRITE (2"DAT2PT) (DATA(N), N=1,64)
     750
              CONTINUE
              DO 780 K=1,64
              DAT2PT=1
                DO 760 I=1,64
                READ (2°DAT2PT) (DATBUF(N), N=1,64)
                DATA(I)=DATBUF(K)
```

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                                                            12
             CONTINUE
   760
           CALL FOURT (DATA, 64, 1, 1, 1, 0)
             DO 770 I=1,64
             COL(I) = (REAL(DATA(I))) + SCALE
             CONTINUE
   770
           WRITE (8'DATBPT) (BCOL(N), N=1,128,2)
   780
           CONTINUE
           ENDFILE 2
           ENDFILE 8
           WRITE (6,795)
   795
           FORMAT( DONE IFFT )
   900
           END
   ROUTINES CALLED:
   SETFIL, FOURT , CABS , FLOAT , SQRT , ALOG , REAL
   OPTIONS =/ON,/OP:3
   BLOCK
               LENGTH
                 (045532)*
   MAIN.
           9645
   **COMPILER ---- CORE**
      PHASE
                 USED FREE
   DECLARATIVES 00963 14349
   EXECUTABLES
                03343 11969
   ASSEMBLY
                04731 15221
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SUBROUTINE FOURT (DATA, NN, NDIM, ISIGN, IFORM, WORK)

THE COOLEY-TUKEY FAST FOURIER TRANSFORM IN USASI BASIC FORTRAN

TRANSFORM(K1, K2, ...) = SUM(DATA(J1, J2, ...) *EXP(ISIGN*2*PI*SURT(-1) *((J1=1)*(K1=1)/NN(1)+(J2=1)*(K2=1)/NN(2)+...))), SUMMED FOR ALL J1, K1 BETWEEN 1 AND NN(1), J2, K2 BETWEEN 1 AND NN(2), ETC. THERE IS NO LIMIT TO THE NUMBER OF SUBSCRIPTS. DATA IS A MULTIDIMENSIONAL COMPLEX ARRAY WHOSE REAL AND IMAGINARY PARTS ARE ADJACENT IN STORAGE, SUCH AS FORTRAN IV PLACES THEM. IF ALL IMAGINARY PARTS ARE ZERO (DATA ARE DISGUISED REAL), SET IFORM TO ZERO TO CUT THE RUNNING TIME BY UP TO FORTY PERCENT. OTHERWISE, IFORM = +1. THE LENGTHS OF ALL DIMENSIONS ARE STORED IN ARRAY NN, OF LENGTH NDIM. THEY MAY BE ANY POSITIVE INTEGERS, THO THE PROGRAM RUNS FASTER ON COMPOSITE INTEGERS, AND ESPECIALLY FAST ON NUMBERS RICH IN FACTORS OF TWO. ISIGN IS +1 OR =1. IF A =1 TRANSFORM IS FOLLOWED BY A +1 ONE (OR A +1 BY A -1) THE ORIGINAL DATA REAPPEAR, MULTIPLIED BY NTOT (=NN(1)* NN(2) + ...). TRANSFORM VALUES ARE ALWAYS COMPLEX, AND ARE RETURNED IN ARRAY DATA, REPLACING THE INPUT. IN ADDITION, IF ALL DIMENSIONS ARE NOT POWERS OF TWO, ARRAY WORK MUST BE SUPPLIED, COMPLEX OF LENGTH EQUAL TO THE LARGEST NON 2**K DIMENSION. OTHERWISE, REPLACE WORK BY ZERO IN THE CALLING SEQUENCE. NORMAL FORTRAN DATA ORDERING IS EXPECTED, FIRST SUBSCRIPT VARYING FASTEST. ALL SUBSCRIPTS BEGIN AT ONE.

RUNNING TIME IS MUCH SHORTER THAN THE NAIVE NTDT**2, BEING GIVEN BY THE FOLLOWING FORMULA. DECOMPOSE NTOT INTO 2**K2 * 3**K3 * 5**K5 * ... LET SUM2 = 2*K2, SUMF = 3*K3 + 5*K5 + ... AND NF = K3 + K5 + ... THE TIME TAKEN BY A MULTI-DIMENSIONAL TRANSFORM ON THESE NTOT DATA IS T = TØ + NTOT*(T1+

T2*SUM2+T3*SUMF+T4*NF), ON THE CDC 3300 (FLOATING POINT ADD TIME OF SIX MICROSECONDS), T = 3000 + NTOT*(500+43*SUM2+68*SUMF+320*NF) MICROSECONDS ON COMPLEX DATA, IN ADDITION, THE ACCURACY IS GREATLY IMPROVED, AS THE RMS RELATIVE ERROR IS BOUNDED BY 3*2**(-8)*SUM(FACTOR(J)**1.5), WHERE B IS THE NUMBER OF BITS IN THE FLOATING POINT FRACTION AND FACTOR(J) ARE THE PRIME FACTORS OF NTOT.

PROGRAM BY NORMAN BRENNER FROM THE BASIC PROGRAM BY CHARLES RADER, RALPH ALTER SUGGESTED THE IDEA FOR THE DIGIT REVERSAL. MIT LINCOLN LABORATORY, AUGUST 1967. THIS IS THE FASTEST AND MOST VERSATILE VERSION OF THE FFT KNOWN TO THE AUTHOR. SHORTER PROGRAMS FOUR1 AND FOUR2 RESTRICT DIMENSION LENGTHS TO POWERS OF TWO. SEE -- IEEE AUDIO TRANSACTIONS (JUNE 1967), SPECIAL ISSUE ON FFT.

THE DISCRETE FOURIER TRANSFORM PLACES THREE RESTRICTIONS UPON THE DATA.

1. THE NUMBER OF INPUT DATA AND THE NUMBER OF TRANSFORM VALUES MUST BE THE SAME.

2. BOTH THE INPUT DATA AND THE TRANSFORM VALUES MUST REPRESENT

EQUISPACED POINTS IN THEIR RESPECTIVE DOMAINS OF TIME AND FREQUENCY. CALLING THESE SPACINGS DELTAT AND DELTAF, IT MUST BE

```
TRUE THAT DELTAF=2*PI/(NN(I)*DELTAT). OF COURSE, DELTAT NEED NOT
      BE THE SAME FOR EVERY DIMENSION.
C
          CONCEPTUALLY AT LEAST, THE INPUT DATA AND THE TRANSFORM OUTPUT
C
C
      REPRESENT SINGLE CYCLES OF PERIODIC FUNCTIONS.
C
C
      EXAMPLE 1. THREE-DIMENSIONAL FORWARD FOURIER TRANSFORM OF A
C
      COMPLEX ARRAY DIMENSIONED 32 BY 25 BY 13 IN FORTRAN IV.
C
      DIMENSION DATA(32,25,13), WORK(50), NN(3)
C
      COMPLEX DATA
      DATA NN/32, 25, 13/
C
C
      DO 1 I=1,32
C
      DO 1 J=1,25
000
      DO 1 K=1,13
      DATA(I, J, K) = COMPLEX VALUE
      CALL FOURT (DATA, NN, 3, -1, 1, WORK)
C
      EXAMPLE 2. ONE-DIMENSIONAL FORWARD TRANSFORM OF A REAL ARRAY OF LENGTH 64 IN FORTRAN II.
C
C
C
      DIMENSION DATA(2,64)
C
      DO 2 I=1,64
C
      DATA(1, I) = REAL PART
C
      DATA(2,1)=0.
C
      CALL FOURT (DATA, 64, 1, -1, 0, 0)
C
      DIMENSION DATA(1), NN(1), IFACT(32), WORK(1)
C
      CDC 6600 INITIALIZATION
      WRED.
      WI=0.
      WSTPR=0.
      WSTPIRO.
      TWOPI=6,283185307
      IF (NDIM-1) 920, 1, 1
1
      NTOT=2
      DO 2 IDIM#1, NDIM
      IF(NN(IDIM))920,920,2
2
      NTOT=NTOT+NN(IDIM)
C
C
      MAIN LOOP FOR EACH DIMENSION
      NP1=2
      DO 910 IDIM=1, NDIM
      N=NN(IDIM)
      NP2=NP1+N
      IF(N=1)920,900,5
Č
      FACTOR N
      MEN
      NTWOSNP1
      IF=1
      IDIV=2
      IQUOT=M/IDIV
10
      IREM=M=IDIV+IQUOT
      IF (IQUOT-IDIV) 50, 11, 11
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     11
           IF (IREM) 20, 12, 20
     12
           NTWOSNTWO+NTWO
           M=1QUOT
3
           GO TO 10
)
     28
           IDIV=3
     30
           IQUOT=M/IDIV
           IREMSM-IDIV+IQUOT
           IF (IQUOT-IDIV) 60, 31, 31
     31
           IF (IREM) 40, 32, 40
     32
           IFACT(IF)=IDIV
           IF=IF+1
           MEIQUOT
           GO TO 30
           IDIV#IDIV+2
     40
           GO TO 30
     50
           IF (IREM) 60,51,60
           NTWO=NTWO+NTWO
     51
           GO TO 70
     60
           IFACT(IF)=M
           SEPARATE FOUR CASES --
     C
               1. COMPLEX TRANSFORM OR REAL TRANSFORM FOR THE 4TH, 5TH, ETC.
     C
                  DIMENSIONS.
     C
              2. REAL TRANSFORM FOR THE 2ND OR 3RD DIMENSION.
                                                                    METHOD --
                  TRANSFORM HALF THE DATA, SUPPLYING THE OTHER HALF BY CON-
     C
                  JUGATE SYMMETRY.
     C
              3. REAL TRANSFORM FOR THE 1ST DIMENSION, N ODD.
                                                                    METHOD --
     C
                  TRANSFORM HALF THE DATA AT EACH STAGE, SUPPLYING THE DTHER
                  HALF BY CONJUGATE SYMMETRY.
     C
     C
               4. REAL TRANSFORM FOR THE 1ST DIMENSION, N EVEN. METHOD--
     C
                  TRANSFORM A COMPLEX ARRAY OF LENGTH N/2 WHOSE REAL PARTS
     CC
                  ARE THE EVEN NUMBERED REAL VALUES AND WHOSE IMAGINARY PARTS
                  ARE THE ODD NUMBERED REAL VALUES. SEPARATE AND SUPPLY
     C
                  THE SECOND HALF BY CONJUGATE SYMMETRY.
     70
           NONZ=NP1*(NP2/NTWO)
           ICASE=1
           IF (IDIM-4) 71, 90, 90
     71
           IF (IFORM) 72, 72, 90
     72
           ICASE#2
           IF(IDIM-1)73,73,90
     73
           ICASE=3
           IF (NTWO-NP1) 90, 90, 74
     74
           ICASE#4
           NTWOSNTW0/2
           N=N/2
           NP2=NP2/2
           NTOT=NTOT/2
           1=3
           DO 88 J=2, NTOT
           DATA(J)=DATA(I)
     80
           I=I+2
     90
           I1RNG=NP1
           IF (ICASE-2) 100, 95, 100
     95
           IIRNG=NPØ+(1+NPREV/2)
```

IF (MMAX-NP2HF) 370,600,600

THETA==TWOPI*FLOAT(NON2)/FLOAT(4*MMAX)

LMAX=MAXØ(NON2T, MMAX/2)
IF(MMAX=NON2) 405, 405, 380

IF (ISIGN) 400, 390, 390

THETA - THETA

WR=COS(THETA)

360 370

380

390

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           WISSIN(THETA)
)
           WSTPR==2. *WI*WI
1
           WSTPI=2. +WR+WI
     405
           DO 570 L=NON2, LMAX, NON2T
           MEL
           IF (MMAX-NON2) 420, 420, 410
5
     410
           W2R#WR*WR=WI*WI
           W21=2. *WR*WI
           W3R#W2R+WR-W2I+WI
           W3I=W2R+WI+W2I+WR
     420
           DO 530 I1=1, I1RNG, 2
           DO 530 J3=11, NON2, NP1
           KMIN#J3+IPAR*M
            IF (MMAX=NON2) 430, 430, 440
;
     430
           KMIN#J3
           KDIF=IPAR*MMAX
     440
     450
           KSTEP=4*KDIF
           DO 520 KI=KMIN, NTOT, KSTEP
           K2=K1+KDIF
           K3=K2+KDIF
            K4=K3+KDIF
           IF (MMAX-NON2) 460, 460, 480
     460
           U1R=DATA(K1)+DATA(K2)
           U11=DATA(K1+1)+DATA(K2+1)
           UZR=DATA(K3)+DATA(K4)
           U2I=DATA(K3+1)+DATA(K4+1)
           U3R=DATA(K1) -DATA(K2)
           U3I=DATA(K1+1)=DATA(K2+1)
           IF (ISIGN) 470, 475, 475
     470
           U4R=DATA(K3+1)=DATA(K4+1)
           U4I=DATA(K4)=DATA(K3)
           GO TO 510
     475
           U4R#DATA(K4+1) -DATA(K3+1)
           U41=DATA(K3)=DATA(K4)
           GO TO 510
     480
            TZR#W2R*DATA(K2) +W2I*DATA(K2+1)
            T2I=W2R*DATA(K2+1)+W2I*DATA(K2)
            T3R=WR*DATA(K3)~WI*DATA(K3+1)
            T3I=WR*DATA(K3+1)+WI*DATA(K3)
            T4R=W3R*DATA(K4)=W3I*DATA(K4+1)
            T4I=W3R*DATA(K4+1)+W3I*DATA(K4)
            U1REDATA(K1)+T2R
           U1I=DATA(K1+1)+T2I
            U2R=T3R+T4R
            U21=T31+T41
            U3R=DATA(K1)=T2R
           U31#DATA(K1+1)#T2I
            IF (ISIGN) 490, 500, 500
     490
            U4R=T3I-T4I
            U4I=T4R-T3R
            GO TO 510
     500
            U4R#T4I#T3I
            U4I=T3R-T4R
     510
            DATA(K1)=U1R+U2R
```

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                                                                  6
           DATA(K1+1) = U1 I+U2 I
           DATA(K2)=U3R+U4R
           DATA(K2+1)=U3I+U4I
           DATA(K3)=U1R=U2R
           DATA(K3+1)=U1I=U2I
           DATA(K4)=U3R+U4R
     520
           DATA(K4+1)=U3I=U4I
           KMIN=4+(KMIN=J3)+J3
           KD1F=KSTEP
           IF (KDIF-NP2) 450, 530, 530
     530
           CONTINUE
           MEXAMMEM
           IF (ISIGN) 540, 550, 550
     540
           TEMPREWR
           WR==WI
           WI == TEMPR
           GO TO 560
     550
           TEMPRENR
           WREWI
           WISTEMPR
     560
           IF (M-LMAX) 565, 565, 410
     565
           TEMPREWR
           WR=WR*WSTPR=WI*WSTPI+WR
     570
           WI=WI*WSTPR+TEMPR*WSTPI+WI
           IPAR=3-IPAR
           MMAX=MMAX+MMAX
           GO TO 360
     C
           MAIN LOOP FOR FACTORS NOT EQUAL TO TWO. APPLY THE TWIDDLE FACTOR
     Ç
           W=EXP(ISIGN+2+PI+SQRT(-1)+(J2-1)+(J1-J2)/(NP2+IFP1)), THEN
     C
           PERFORM A FOURIER TRANSFORM OF LENGTH IFACT(IF), MAKING USE OF
     C
           CONJUGATE SYMMETRIES,
     C
     600
           IF (NTWO-NP2) 605, 700, 700
     605
           IFP1=NON2
           IF=1
           NP1HF=NP1/2
           IFP2=IFP1/IFACT(IF)
     610
           J1RNG=NP2
           IF (ICASE=3)612,611,612
     611
           JIRNG=(NP2+IFP1)/2
           J2STP=NP2/IFACT(IF)
           J1RG2=(J2STP+IFP2)/2
     612
           J2MIN=1+IFP2
           IF (IFP1-NP2)615,640,640
     615
           DO 635 J2=J2MIN, IFP1, IFP2
           THETA==TWOPI*FLOAT(J2=1)/FLOAT(NP2)
           IF (ISIGN) 625, 620, 620
     620
           THETA -THETA
     625
           SINTH=SIN(THETA/2.)
           WSTPR==2. +SINTH+SINTH
           WSTPI#SIN(THETA)
           WREWSTPR+1.
           WIEWSTPI
```

A COMPANY

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'RAN VØ6.13
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           J1MIN=J2+IFP1
           DO 635 J1=J1MIN, J1RNG, IFP1
           I1MAX=J1+I1RNG=2
           DO 630 I1=J1, I1MAX, 2
           DO 630 13=11, NTOT, NP2
           J3MAX=I3+IFP2-NP1
           DO 630 J3=13, J3MAX, NP1
           TEMPR=DATA(J3)
           DATA(J3)=DATA(J3)*WR=DATA(J3+1)*WI
    630
           DATA(J3+1) = TEMPR * WI+DATA(J3+1) * WR
           TEMPREWR
           WR=WR*WSTPR•WI*WSTPI+WR
    635
           WI=TEMPR*WSTPI+WI*WSTPR+WI
    640
           THETA==TWOPI/FLOAT(IFACT(IF))
           IF(ISIGN)650,645,645
    645
           THETA = THETA
    650
           SINTH#SIN(THETA/2.)
           WSTPR==2. +SINTH+SINTH
           WSTPISSIN(THETA)
           KSTEP=2*N/IFACT(IF)
           KRANG=KSTEP*(IFACT(IF)/2)+1
           DO 698 I1=1, I1RNG, 2
           DO 698 13=11, NTOT, NP2
           DO 690 KMIN=1, KRANG, KSTEP
           J1MAX=I3+J1RNG=IFP1
           DO 680 J1=13, J1MAX, IFP1
           J3MAX=J1+IFP2=NP1
           DO 680 J3=J1, J3MAX, NP1
           J2MAX=J3+IFP1=IFP2
           K=KMIN+(J3-J1+(J1-I3)/IFACT(IF))/NP1HF
1
           IF (KMIN-1)655,655,665
     655
           SUMR=0.
           SUMISO.
           DO 660 J2=J3, J2MAX, IFP2
           SUMR=SUMR+DATA(J2)
     660
           SUMI=SUMI+DATA(J2+1)
           WORK(K)=SUMR
           WORK(K+1)=SUMI
           GO TO 680
           KCONJ=K+2*(N=KMIN+1)
     665
           J2=J2MAX
           SUMREDATA (J2)
           SUMI=DATA(J2+1)
           OLDSR=0.
           OLDSI=0.
           J2=J2-IFP2
           TEMPR=SUMR
     670
           TEMPI = SUMI
           SUMRETWOWR & SUMR = OLDSR + DATA (J2)
           SUMI = TWOWR + SUMI = OLDSI + DATA (J2+1)
           OLDSR = TEMPR
           OLDSI=TEMPI
           J2=J2=IFP2
           IF(J2-J3)675,675,670
```

TEMPR=WR+SUMR=OLDSR+DATA(J2)

675

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'RAN VØ6.13
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                                                                  8
           TEMPI=WI + SUMI
           WORK(K)=TEMPR=TEMPI
           WORK (KCONJ) = TEMPR+TEMPI
           TEMPR=WR+SUMI=OLDSI+DATA(J2+1)
           TEMPI=WI+SUMR
           WORK(K+1)=TEMPR+TEMPI
           WORK (KCONJ+1) = TEMPR = TEMPI
           CONTINUE
    680
           IF (KMIN-1) 685, 685, 686
           WR=WSTPR+1.
    685
           WI=WSTPI
           GO TO 690
    686
           TEMPR=WR
           WR=WR*WSTPR=WI*WSTPI+WR
           WI=TEMPR * WSTPI+WI * WSTPR+WI
    690
           TWOWR=WR+WR
           IF (ICASE=3)692,691,692
    691
           IF (IFP1=NP2)695,692,692
    692
           K=1
           IZMAX=I3+NP2=NP1
           DO 693 12=13,12MAX,NP1
           DATA(12)=WORK(K)
           DATA(12+1) #WORK(K+1)
    693
           K=K+2
           GO TO 698
    C
           COMPLETE A REAL TRANSFORM IN THE 1ST DIMENSION, N ODD, BY CON-
    C
    C
           JUGATE SYMMETRIES AT EACH STAGE.
    695
           J3MAX=I3+IFP2=NP1
           DO 697 J3=13, J3MAX, NP1
           J2MAX=J3+NP2=J2STP
           DO 697 J2=J3, J2MAX, J2STP
           J1MAX=J2+J1RG2=IFP2
           J1CNJ#J3+J2MAX+J2STP#J2
           DO 697 J1=J2, J1MAX, IFP2
           K=1+J1+I3
           DATA(J1)=WORK(K)
           DATA(J1+1) = WORK(K+1)
           IF (J1+J2)697,697,696
    696
           DATA(J1CNJ)=WORK(K)
           DATA(J1CNJ+1) == WORK(K+1)
    697
           J1CNJ#J1CNJ#IFP2
    698
           CONTINUE
           IF=IF+1
           IFP1=IFP2
           IF (IFP1-NP1) 700, 700, 610
    C
           COMPLETE A REAL TRANSFORM IN THE 1ST DIMENSION, N EVEN, BY CON-
    C
           JUGATE SYMMETRIES.
           GO TO (900,800,900,701), ICASE
    700
           NHALFEN
     701
           N=N+N
```

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IF (I-IMAX) 750, 760, 760 760 DATA(J)=DATA(IMIN)=DATA(IMIN+1) DATA(J+1)=0. IF (I-J) 770, 780, 780 DATA(J)=DATA(I) 765 DATA(J+1) = DATA(I+1) 770 I=1-5 J=J=2 IF (1. IMIN) 775, 775, 765 775 DATA(J)=DATA(IMIN)+DATA(IMIN+1)

'RAN V06.13

702 703

710

720

725

730

731 735

740

745

750

755

THETA == THETA

WREWSTPR+1. WI=WSTPI IMIN=3

J=JMIN

J=J+NP2 IMIN=IMIN+2 JMINEJMIN-2 TEMPR=WR

NP2=NP2+NP2 NTOT=NTOT+NTOT

IMAX=NTOT/2+1

J=NTOT+1

I=IMIN GO TO 755

I=1+2 J=J=2

JMIN=2*NHALF=1 GO TO 725

```
'RAN VØ6.13
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                                                                10
           DATA(J+1)=0.
;
           IMAX=IMIN
,
           GO TO 745
     780
3
           DATA(1)=DATA(1)+DATA(2)
)
           DATA(2)=0.
,
           GO TO 900
     C
           COMPLETE A REAL TRANSFORM FOR THE 2ND OR 3RD DIMENSION BY
     C
     C
           CONJUGATE SYMMETRIES.
     C
     800
           IF (I1RNG-NP1)805,900,900
           DO 860 13=1, NTOT, NP2
     805
           I2MAX=I3+NP2-NP1
           DO 860 12=13,12MAX,NP1
           IMIN=12+11RNG
           IMAX=12+NP1=2
           JMAX=2*13+NP1=IMIN
           IF(I2-13)820,820,810
     810
           SAN+XPMC=XPMF
     820
           IF (IDIM-2) 850, 850, 830
     830
           J=JMAX+NPØ
           DO 840 I=IMIN, IMAX, 2
           DATA(I)=DATA(J)
           DATA(I+1) == DATA(J+1)
     840
           J=J=2
     850
           J=JMAX
           DO 860 I=IMIN, IMAX, NPO
           DATA(I) = DATA(J)
           DATA(I+1) == DATA(J+1)
     860
           J=J=NP0
     CCC
           END OF LOOP ON EACH DIMENSION
     C
     900
           NP0=NP1
           NP1=NP2
     910
           NPREVEN
           RETURN
     920
           END
     ROUTINES CALLED:
     MAXO , FLOAT , COS
                            , SIN
     OPTIONS =/ON,/OP:3
     BLOCK
                  LENGTH
     FOURT
             3472 (015440)*
     **COMPILER **** CORE**
        PHASE
                    USED FREE
     DECLARATIVES 00622 14690
     EXECUTABLES
                   01583 13729
     ASSEMBLY
                   02435 17517
```

User's Guide

File Structures

SPU FILDMP

FILDMP U007B

SKB1/EMKDPO1PROCSD.IMG

| The color of the

SPU FILDMP

FILDMP U007B

#KB4 OCKDPOAFFTCOF NRM

FFTCOF.NRM (OCTAL)

Vita

Dennis A. McGaugh was born on November 9, 1947 in Eugene, Oregon. He graduated from South Eugene High School in 1966. After spending three years at Oregon State University, he was drafted into the Army in 1969. He received basic and advanced infantry training at Ft. Ord, California and then entered Infantry Officer's Candidate School at Ft. Benning, Georgia where he graduated in November 1970, and was commissioned a Second Lieutenant in Military Intelligence. During his first assignment at NSA, Ft. Meade, Maryland, he attended the John Hopkins University, Baltimore and graduated in September 1973 with a Bachelor of Science in Mechanical Engineering. His next assignment was to USASA Field Station, Korea, were he served a the operations officer of the 146th ASA Aviation Company from October 1974 until November 1975. He then attended the US Army Military Intelligence Officer's Advanced Course at Ft. Huadruca, Arizonia before entering the Air Force Institute of Technology in September 1976.

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A FORTRAN program is presented that will interactively prepare	
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digital preparation includes the ability to Discrete Fourier	
Transform (DFT), Inverse Fourier Transform (IDFT), threshold	
image power spectral density, and to perform two-dimensional	
image filtering. Further, a brief dis	cussion of image dis-
tortion measurements, optimal image si	ze for experimental
	()